# Explicit Koszul-dualizing bimodules in bordered Heegaard Floer homology 

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## Supplement: Cancellation diagrams

In these diagrams, $d$-arrows are labeled $d$, ordinary $H$-arrows are labeled $H$, and special $H$-arrows are labeled $H_{s p}$.


Figure 1: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 2: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Case 2.1
Figure 3: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 4: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.





$\downarrow d$

$\downarrow d$

Case 2.5(a)
(20)


Figure 5: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 6: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 7: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Cases 2.7(a) and 2.8(a) are exactly the same as Cases 2.1 and 2.2.


Case 2.9(b)
Figure 8: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Case 2.9(a) is exactly the same as Case 2.3.



Case 3.3
Figure 10: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 11: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 12: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 13: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 14: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Cases 4.7(a) and 4.8(a) are similar to Cases 2.5(a) and 2.6(a).


Figure 15: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 16: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Case 4.10(a) is the same as Case 4.1.


Figure 17: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Case 4.11(a) is the same as Case 4.2.


Figure 18: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Case 4.12(a) is the same as Case 4.3.


Case 4.13(b)
Figure 19: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$. Case 4.13(a) is the same as Case 4.4. Case 4.13(c), with the second special case, cannot occur.


Case 6.1
Figure 20: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 21: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 22: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 23: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Case 10.1
Figure 24: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Figure 25: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Case 11.3


Case 11.4

Figure 26: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.


Case 11.5
Figure 27: Cancellations in $d \circ H+H \circ d=\mathbb{I}_{M}$.

